

University of Petra



Faculty of Information Technology

كلية تكنولوجيا المعلومات

Department of Computer Science

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Advanced Algorithms
601326

Midterm Exam – 2025 1

Your ID:



Your Instructor Name:

Instructions for the Exam:

- Write your name and ID number on the exam and answer sheets.
- Write the number of the section that you enrolled in.
- Write the name of your instructor.
- Questions in the exam not allowed.
- Using any type of technology (mobiles, smart watches) not allowed
- Using extra papers or sheets not allowed
- The exam consists of Six questions.

For instructor use only:

| Question number | Course ILO | Program ILO | Question weight | Student mark |
|-----------------|------------|-------------|-----------------|--------------|
| Q1 | | | 4 | 2 |
| Q2 | K2 | | 4 | 3 |
| Q3 | I1 | | 8 | 3.75 |
| Q4 | | | 5 | 3.75 |
| Q5 | | | 5 | 4.5 |
| Q6 | | | 4 | 3 |
| Total /30 | | | | 20 |

Q1) Discuss median-of-three pivot selection and how it enhances Quick Sort algorithm worst case. (4 marks)

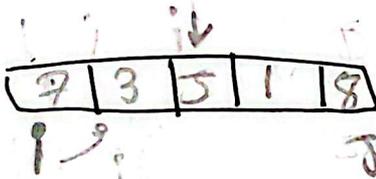
2

```

quicksort(A, L, R)
  if L < R
    partition = partition(A, L, R)
    quicksort(A, L, partition-1)
    quicksort(A, partition+1, R)

partition(A, L, R)
  pivot = (L+R)/2
  i = L-1
  
```

hoare



~~You may take the pivot to be the...~~

~~When picking the pivot to be in the middle it's going to take longer time to sort since the amount of swaps could be more~~

* worst case in the quick sort shows ~~with~~ when the right place for the partition is near the far right or the far left, cases when that happen it's like you're working with an array of size $(N-1)$ which doesn't really make diff. from sorting an array of size N

- the point of the tech used in it ~~is~~ -designed and you're trying to make small by half or divide the half

$O(n^2)$??

3

Q2) Consider the following algorithm.

(4 marks)

```

Algorithm XYZ (A [0..n - 1])
//Input: An array A[0..n - 1] of n real numbers
val ← 10
res1 ← 0
res2 ← 1
for i ← 0 to n - 1 do
  if A[i] >= val
    res1 ← A[i] + res1
  if A[i] < val/2
    res2 ← A[i] * res2
return res1 - res2

```

- What does this algorithm compute?
- What is the time complexity for the algorithm?

b $T(n) = 1 + 1 + 1 + n + n + n + n + n + 1$
 $T(n) = 5n + 4$ O(?)

as it goes in a for loop of the size of the element in the array in the number in the index it's n is bigger than val it changes res1 to be that number + res1 and if the number in that index is less than val/2 it changes the value of res2 to be the value of that number multiplied by val after exiting the loop it returns the value of res1 - res2



3.75

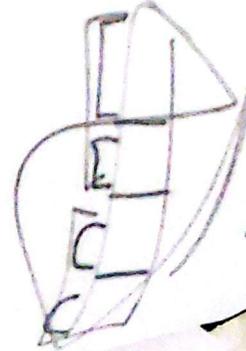
Q3) Design a divide-and-conquer algorithm to compute the summation of elements in an array. (8 marks)
 Setup and solve a recurrence relation for the number of summations made by your algorithm (use Master Theorem)

~~Sum(A) {
 n = A.length
 k = 1
 for i = 0 to n
 sum(A[i])
 return sum~~

Sum(A) {
 k = A.length
 m = k/2
 Sum(m) + Sum(m)



next algo that sum numbers in arr



```

Sum(n, A)
if m == 0
    return 0
else
    n = n/2
    Sum(n, A)

```

$$T(n) = 2T\left(\frac{n}{2}\right) + f(n)$$

$$T(n) = O\left(\frac{n}{2}\right) + \frac{1}{2}$$

0.75

```

Sum(n, A) // length of array
if n == 1;
    return A[0];
else
    m = n/2

```

3

```

//
// Sum | = 0 to m
Sum(n, A)
if (s = 1 + A[s]) for f = m to n
    Sum(n, A)
    ← s = k + A[s]

```

Q4) Consider the following recursive algorithm:

(5 marks)

```

Algorithm Q(n)
//Input: A positive integer n
if n = 1
  return 1
else
  return Q(n - 1) + 2 * n - 1
  
```

3.75

- Setup a recurrence relation for the number of multiplications made by this algorithm.
- Solve the recurrence relation using backward substitution and find Big O.

$$T(n) = \begin{cases} 0, n=1 \\ T(n-1) + 2, n > 1 \end{cases}$$

1.75

using base case:

$$T(1) = 0$$

$$n-i=0$$

$$n=1$$

2

$$T(n) = T(n-1) + 2(n-1)$$

$$T(n-1) = T(n-2) + 2(n-2)$$

$$T(n-2) = T(n-3) + 2(n-3)$$

$$T(n) = T(n-3) + 2(n-3) + 2(n-2) + 2(n-1)$$

$$\text{Let } i=1$$

$$T(n-i) + \sum_{i=3}^n n-i$$

$$T(n-n) + \sum_{i=1}^n n-i$$

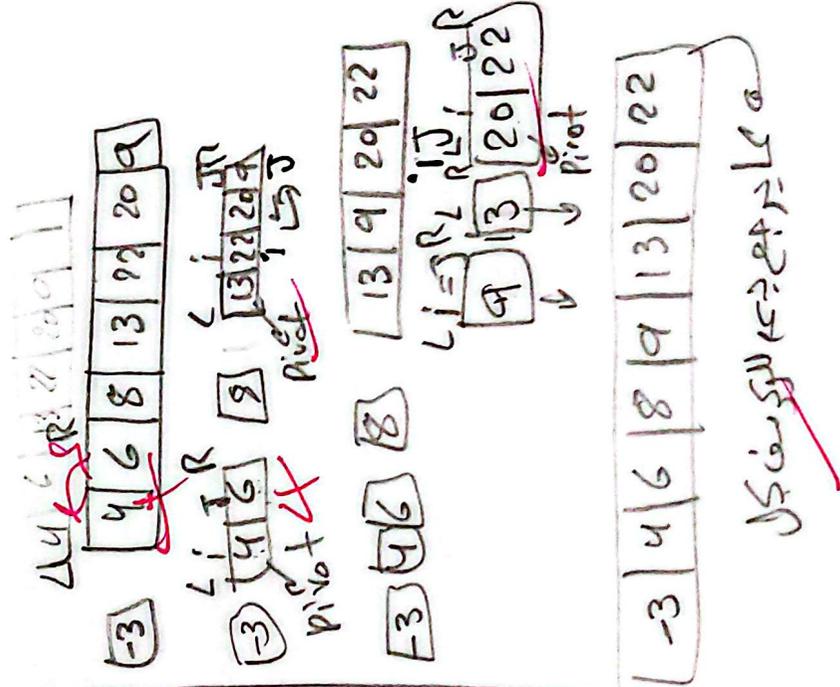
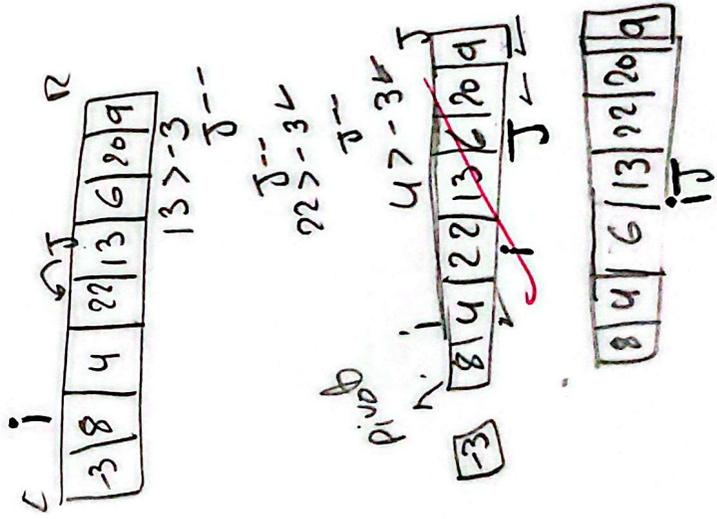
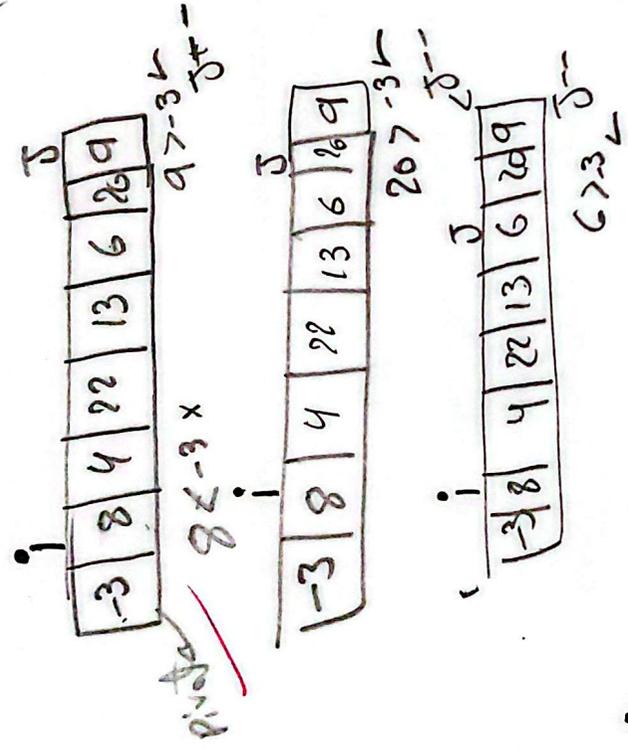
$$1 + \sum_{i=1}^n n-i = \frac{n(n+1)}{2}$$

$$T(n) = 1 + n - \frac{n^2+1}{2}$$

$$O(n^2)$$

4.5

Q5) Given the following array, $A = -3, 8, 4, 22, 13, 6, 20, 9$
 Apply Quick Sort algorithm to sort the array elements in ascending order (show detailed steps) (5 marks)



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Q6) Based on your understanding of the covered algorithms, answer the following: (4 marks)

a) Compare Selection Sort to Sequential Search algorithms in terms of best and worst cases.

| | Selection sort | Sequential search |
|------------|----------------|-------------------|
| Best case | $O(n^2)$ ✓ | $O(1)$ ✓ |
| Worst case | $O(n^2)$ ✓ | $O(n)$ ✓ |

b) Discuss briefly the Best Case of Insertion Sort algorithm.

Best case: when the array is sorted in the order you want

cus then you wouldn't have to go through the swapping with loop - since it's sorted it's going to compare it only with the first number on it's right, finds it smaller - then goes to the next index ✓

